

Dynamic Merger Review*

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Abstract

We analyze the optimal dynamic policy of an antitrust authority towards horizontal mergers when merger proposals are endogenous and occur over time. Approving a currently proposed merger will affect the profitability and welfare effects of potential future mergers, the characteristics of which may not yet be known to the antitrust authority. We show that, in many cases, this apparently difficult problem has a simple resolution: an antitrust authority can maximize discounted consumer surplus by using a completely myopic merger review policy that approves a merger today if and only if it does not lower consumer surplus given the current market structure.

1 Introduction

The traditional approach to the review of horizontal mergers stresses the tradeoff between market power and efficiencies. Mergers, which cause firms to internalize pricing externalities among former rivals, increase the exercise of market power, and therefore tend to reduce social welfare. On the other hand, since they

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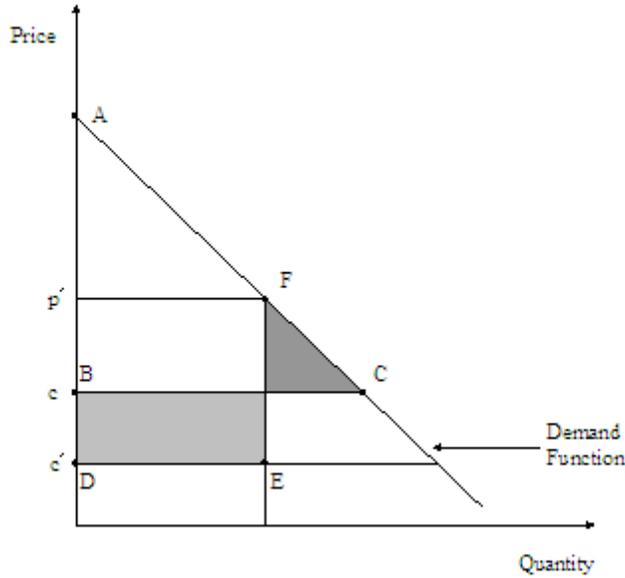


Figure 1: The Williamson tradeoff of merger approval: deadweight loss of market power (dark-shaded triangle) *vs.* efficiency gain (light-shaded rectangle).

can create efficiencies, horizontal mergers may instead increase welfare. This tradeoff was first articulated by Williamson [1968] for the case of an antitrust authority who wants to maximize aggregate surplus, using a diagram like Figure 1. In the diagram, a competitive industry merges to become a monopolist that charges the price p' , but lowers its marginal cost of production from c to c' . Whether aggregate surplus increases or not depends on whether the dark-grey deadweight loss triangle exceeds the light-grey efficiency gain. A similar, though even more straightforward tradeoff arises when an antitrust authority instead applies a consumer surplus standard to merger approval decisions.¹ In that case, the marginal cost reduction must be large enough that the price does not increase for the merger to be approved.

More recently, Farrell and Shapiro [1990] (see also McAfee and Williams [1992]) have provided a more complete and formal analysis of this tradeoff for the context of Cournot competition. Farrell and Shapiro provide a necessary and sufficient condition for a merger to increase consumer surplus, as well as a sufficient condition for a merger to increase aggregate surplus.

With few exceptions, however, the literature on merger review has focused on

¹Note that in both the U.S. and the EU, the legal standard of merger policy is close to being a consumer surplus standard rather than an aggregate surplus standard.

the approval decision for a single merger. Yet, in reality, mergers are usually not one-time events.² That is, one proposed merger in an industry may be followed by others. In that case, approval of a merger today based on current conditions, as in the Farrell and Shapiro test, appears inappropriate. Rather, an antitrust authority in general needs to determine the welfare effect of the current proposed merger given the potential for future merger approvals, and given the fact that today's merger approval decision may alter the set of mergers that are later proposed.

In this paper, we show that in some cases this apparently difficult problem has a very simple resolution: an antitrust authority who wants to maximize consumer surplus can accomplish this objective by using a completely myopic merger review policy that approves a merger today if and only if it does not lower consumer surplus given the current market structure.

We begin in Section 2 by describing our basic model and establishing some preliminary characterizations of consumer surplus-enhancing mergers and their interactions. Our central results focus on a model of Cournot competition with constant returns to scale. Most importantly, we show in this section that there is a form of complementarity among consumer surplus-enhancing mergers in this setting.

Section 3 contains our main result. There we imbed our Cournot competition framework in a dynamic model in which merger opportunities arise, and may be proposed, over time. We show that if the set of possible mergers is disjoint, and if mergers that are not approved in a given period may be approved at a later date, then a completely myopic consumer surplus-based approval policy maximizes discounted consumer surplus for every possible realization of the set of feasible mergers.

In Section 4 we discuss the robustness of this result, considering other models of competition (homogeneous and differentiated product price competition), nonconstant returns to scale, nondisjointness of mergers, and the use of an aggregate surplus criterion. [NEED TO COMPLETE THIS PARA]

Section 5 concludes.

2 Mergers in the Cournot Model

2.1 Cournot Oligopoly

Consider an industry with n firms producing a homogeneous good and competing in quantities. Let $N \equiv \{1, 2, \dots, n\}$ denote the set of firms. Firm i 's cost of producing q_i units of output is given by $C_i(q_i) = c_i q_i$. Thus, for now, we restrict attention to firms producing under constant returns to scale. The inverse market demand is given by the twice differentiable function $P(Q)$, where

²Motta and Vasconcelos [2005] is the one paper we are aware of that considers merger review in a dynamic context. Nilssen and Sorgard [1998], Gowrisankaran [1999], Fauli-Oller [2000], and Pesendorfer [2005] are among the articles that study equilibrium merger decisions in dynamic settings without considering merger policy (and, usually, without allowing for efficiencies).

$Q \equiv \sum_{i \in N} q_i$ is industry output. We make the following (standard) assumption on demand.³

Assumption 1 For any $Q > 0$ such that $P(Q) > 0$:

- (i) $P'(Q) < 0$;
- (ii) $P'(Q) + QP''(Q) < 0$;
- (iii) $\lim_{Q \rightarrow \infty} P(Q) < \min_i c_i$;
- (iv) $\lim_{Q \rightarrow 0} P(Q) > \min_i c_i$.

Part (i) of the assumption says that demand is downward-sloping, part (ii) implies that quantities are strategic substitutes and that each firm's profit maximization problem is strictly concave, parts (iii) and (iv) imply that the equilibrium aggregate output is positive but bounded.

Let $Q_{-i} \equiv \sum_{j \neq i} q_j$ denote the aggregate output of all firms other than i . Firm i 's best-response function, $b(Q_{-i}; c_i)$, is

$$b(Q_{-i}; c_i) = \arg \max_{q_i} [P(Q_{-i} + q_i) - c_i]q_i. \quad (1)$$

As is well known (see e.g., Farrell and Shapiro [1990]), Assumption 1 implies that each firm's best-response function $b(\cdot; c_i)$ satisfies $\partial b(Q_{-i}; c_i) / \partial Q_{-i} \in (-1, 0)$ at all Q_{-i} such that $b(Q_{-i}; c_i) > 0$.

Under Assumption 1, there is a unique Nash equilibrium. Let Q^* and q_i^* denote industry output and firm i 's output in equilibrium. From the first-order condition for problem (1), output levels in this equilibrium satisfy

$$q_i^* = -\frac{P(Q^*) - c_i}{P'(Q^*)} \quad (2)$$

if $c_i < P(Q^*)$, and $q_i^* = 0$ otherwise. Assumption 1 also implies that the equilibrium is "stable," so that comparative statics are "well behaved." For example, we will make use of two comparative statics properties: First, a reduction in an active firm's marginal cost increases its equilibrium output and profit, reduces the output of each of its active rivals, and increases aggregate output. Second, following any change in the incentives of a subset of firms, the equilibrium aggregate output increases [decreases] if and only if the equilibrium output of that set of firms increases [decreases].⁴

2.2 The CS-Effect of Mergers

Consider a merger between a subset $M \subseteq N$ of firms. The post-merger marginal cost is denoted \bar{c}_M . Aggregate output before the merger is Q^* , and after is \bar{Q}^* .

³We assume that this assumption holds for all possible market structures and cost positions that may emerge through the merger review process.

⁴See Farrell and Shapiro [1990]'s Lemma, p. 111.

We are interested in the effect of the merger on consumer surplus, $CS(\bar{Q}^*) - CS(Q^*)$, where

$$CS(Q) = \int_0^Q [P(s) - P(Q)] ds.$$

Since $CS'(Q) = -QP'(Q) > 0$, a merger raises consumer surplus if and only if it induces an increase in industry output. We will say that a merger is *CS-neutral* if the merger does not affect consumer surplus. Similarly, we will say that a merger is *CS-increasing* [*CS-decreasing*], if consumer surplus following the merger is higher [lower] than before. Finally, a merger is *CS-nondecreasing* [*CS-nonincreasing*] if it is not CS-decreasing [CS-increasing].

We will say that a merger involves active firms if at least one of the merging firms is producing a positive quantity before the merger [and hence has $c_i < P(Q^*)$]. Observe that a merger involving only inactive firms is always CS-nondecreasing and weakly profitable. The following result catalogs some useful properties of CS-neutral mergers among active firms.

Lemma 1 *If a merger involving active firms is CS-neutral then*

1. *it causes no changes in the output of any nonmerging firm nor the total output of the merging firms;*
2. *the merged firm's margin at the pre-merger price $P(Q^*)$ equals the sum of the active merging firms' pre-merger margins:*

$$P(Q^*) - \bar{c}_M = \sum_{i \in M} \max\{0, P(Q^*) - c_i\}; \quad (3)$$

3. *the merged firm's marginal cost is no greater than the marginal cost of the most efficient merger partner: $\bar{c}_M \leq \min_{i \in M} \{c_i\}$, and it is strictly less if the merger involves at least two active firms;*
4. *the merger is profitable (it weakly raises the joint profit of the merging firms), and is strictly profitable if it involves at least two active firms.*

Proof. To see Property 1, observe that under Assumption 1 there is a unique output level for each non-merging firm i that is compatible with any given level of aggregate output Q [since there is a unique Q_{-i} such that $Q_{-i} + b(Q_{-i}; c_i) = Q$]. Since aggregate output is unchanged by a CS-neutral merger, all nonmerging firms' outputs are unchanged. In turn, this implies that the total output of the merging firms must be unchanged as well. For Property 2, a central feature in Farrell and Shapiro [1990]'s analysis, note that the merged firm's first-order condition is

$$P(Q^*) - \bar{c}_M + \left(\sum_{i \in M} q_i^* \right) P'(Q^*) = 0. \quad (4)$$

Summing up the pre-merger first-order conditions of the active merger partners yields

$$\sum_{i \in M_+} [P(Q^*) - c_i] + \sum_{i \in M_+} q_i^* P'(Q^*) = 0 \quad (5)$$

where $M_+ = \{i \in M : q_i^* > 0\}$. Since for all $i \in M \setminus M_+$, we have $P(Q^*) \leq c_i$ and $q_i^* = 0$, it follows that

$$\sum_{i \in M} \max\{0, P(Q^*) - c_i\} + \left(\sum_{i \in M} q_i^* \right) P'(Q^*) = 0 \quad (6)$$

Combining equations (4) and (6), yields (3). Property 3 follows directly from Property 2. Property 4 holds since the merging firms' joint output has not changed (Property 1), but its margin has weakly increased, and has strictly increased if the merger involves at least two active firms (Property 2). ■

The following useful corollary follows from Properties 2 and 4 of Lemma 1 plus the fact that the post-merger aggregate output, \bar{Q}^* , and the profit of the merged firm are both decreasing in the merged firm's marginal cost, \bar{c}_M :

Corollary 1 *A merger involving active firms is CS-neutral if*

$$\bar{c}_M = \hat{c}_M(Q^*) \equiv P(Q^*) - \sum_{i \in M} \max\{0, P(Q^*) - c_i\},$$

CS-increasing if $\bar{c}_M < \hat{c}_M(Q^)$, and CS-decreasing if $\bar{c}_M > \hat{c}_M(Q^*)$. Moreover, any CS-nondecreasing merger is profitable for the merging firms, and is strictly profitable if it is CS-increasing or involves at least two active firms.*

Thus, an antitrust authority concerned with maximizing consumer surplus and confronted with a single merger involving active firms in set M would want to approve the merger if and only if $\bar{c}_M \leq \hat{c}_M(Q^*)$. Moreover, any merger the antitrust authority would want to approve is profitable for the merging parties and hence will be proposed.

Observe also that the threshold $\hat{c}_M(Q^*)$ is nondecreasing in Q^* ; the larger is Q^* (and the lower is the current price), the more likely it is that a merger is CS-nondecreasing. This fact will play a central role in the next subsection when we look at interactions among mergers. To see the intuition for this result, consider a proposed merger between symmetric firms, each of whom has a pre-merger marginal cost c and produces $q > 0$ units. Since the firms are choosing their outputs optimally before the merger, a lower pre-merger margin $P(Q^*) - c$ (due to a larger pre-merger aggregate output) implies a smaller pre-merger value of $P'(Q^*)q$ [see (2)]. The incentives of the merged firm to raise price, however, depend on a comparison of the merger's marginal cost reduction $\Delta c = (c - \bar{c}_M)$ to the market power effect, $P'(Q^*)q$, which reflects the internalization of the pricing externality between the merging firms. With a CS-nondecreasing merger, the first effect weakly exceeds the second. A smaller pre-merger price preserves this relation and therefore the CS-nondecreasing effect of the merger.

Figure 2 illustrates the cases of CS-neutral, CS-increasing, and CS-decreasing mergers. The figure considers a merger involving the firms in set M_1 . The complementary set of firms is denoted $M_2 \equiv N \setminus M_1$. The axes in the figure measure the joint outputs of the two sets of firms. The curves labeled r_{M_1} and r_{M_2} depict what we call the "group-reaction functions" of each set of firms

prior to the merger. Specifically, M_i 's pre-merger group-reaction function gives the joint pre-merger Nash-equilibrium output of the firms in M_i , $r_{M_i}(q_{M_j})$, conditional on the firms in M_j jointly producing q_{M_j} . It is routine to verify that these group-reaction functions satisfy $-1 < r'_{M_i}(q_{M_j}) < 0$.

The equilibrium before the merger is point A, the intersection of the two pre-merger group-reaction curves. With a CS-neutral merger, the post-merger best-response curve of the merged firm, $b(q_{M_2}; \hat{c}_{M_1}(Q^*))$, intersects group M_2 's group-reaction curve, $r_{M_2}(\cdot)$, at point A.⁵ With a CS-increasing merger, the merged firm's marginal cost is less than $\hat{c}_{M_1}(Q^*)$, so its best-response curve lies further to the right, shifting the equilibrium to point B, where there is a larger aggregate output. In contrast, with a CS-decreasing merger, the merged firm's marginal cost is greater than $\hat{c}_{M_1}(Q^*)$, so its best-response curve lies further to the left, shifting the equilibrium to point C where there is a smaller aggregate output.

2.3 Interactions between Mergers

We now turn to the interactions between mergers. In this subsection, we consider two potential disjoint mergers, involving firms in sets M_1 and M_2 with $M_1 \cap M_2 = \emptyset$. We'll refer to these simply as merger M_1 and merger M_2 . The set of firms not involved in either merger is $N^c \equiv N \setminus (M_1 \cup M_2)$.

Our first result establishes a certain complementarity between mergers that change consumer surplus in the same direction:⁶

Proposition 1 *The sign of the CS-effect of two disjoint mergers is complementary:*

- (i) *if a merger is CS-nondecreasing (and hence profitable) in isolation, it remains CS-nondecreasing (and hence profitable) if another merger that is CS-nondecreasing in isolation takes place;*
- (ii) *if a merger is CS-decreasing in isolation, it remains CS-decreasing if another merger that is CS-nonincreasing in isolation takes place.*

⁵The fact that it lies to the right [left] of the pre-merger group-reaction curve of M_1 for $q_{M_2} > [<]q_{M_2}^*$ can be shown using logic similar to that leading to Corollary 1. Specifically, any post-merger best-response curve for the merged firm must cross the merged firms' pre-merger group-reaction curve once at the non-merging firms' joint output \bar{q}_{M_2} such that $\hat{c}_{M_1}(\bar{q}_{M_2} + r_{M_1}(\bar{q}_{M_2})) = \bar{c}_{M_1}$. Moreover, this crossing must be from above: at $q_{M_2} > [<]\bar{q}_{M_2}$, we have

$$\begin{aligned} b(q_{M_2}; \bar{c}_{M_1}) &= b(q_{M_2}; \hat{c}_{M_1}(\bar{q}_{M_2} + r_{M_1}(\bar{q}_{M_2}))) \\ &> [<]b(q_{M_2}; \hat{c}_{M_1}(q_{M_2} + r_{M_1}(q_{M_2}))) \\ &= r_{M_1}(q_{M_2}). \end{aligned}$$

⁶Proposition 1 focuses on properties we use later in this section. It is straightforward to show as well that a CS-increasing merger remains CS-increasing if a merger that is CS-nondecreasing takes place, and that a merger that is CS-nonincreasing remains CS-nonincreasing if a merger that is CS-nonincreasing takes place.

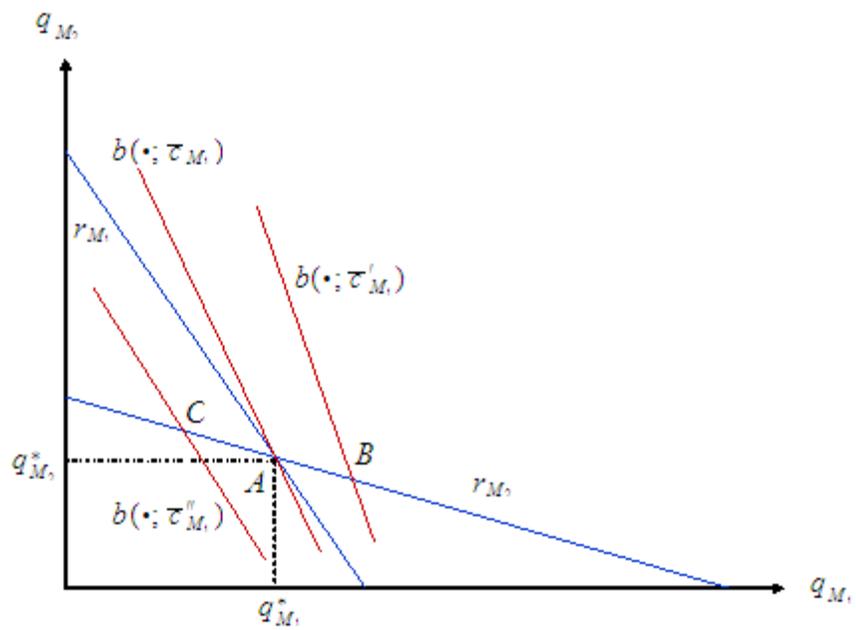


Figure 2: A merger involving the firms in M_1 . Depending on the merged entity's marginal cost, the merger is CS-neutral, CS-increasing, or CS-decreasing. In the figure, $\bar{c}''_{M_1} > \bar{c}_{M_1} > \bar{c}'_{M_1}$.

Proof. For part (i), suppose that mergers M_1 and M_2 are both CS-non-decreasing in isolation. Let Q^* denote aggregate output in the absence of either merger and let \bar{Q}_i^* denote aggregate output if only merger i takes place. So $\bar{Q}_i^* \geq Q^*$ for $i = 1, 2$. Suppose, first, that merger M_i involves only inactive firms. Then since $P(\bar{Q}_j^*) \leq P(Q^*) \leq c_i$, it also involves only inactive firms once merger j takes place. Thus, it remains CS-nondecreasing and (weakly) profitable.

Suppose, instead, that merger M_i involves active firms. From Corollary 1 we know that $\bar{c}_{M_i} \leq \hat{c}_{M_i}(Q^*)$ for $i = 1, 2$. Since the threshold $\hat{c}_{M_i}(Q)$ is nondecreasing in Q , we have $\bar{c}_{M_i} \leq \hat{c}_{M_i}(\bar{Q}_j^*)$ for $i, j = 1, 2, i \neq j$. That is, each merger is also CS-nondecreasing once the other merger has taken place. The argument for part (ii) follows similar lines (note that a CS-decreasing merger must involve active firms). ■

Figure 3 illustrates the complementarity between two mergers that are CS-increasing in isolation when no other firms exist ($N^c = \emptyset$). In isolation, merger M_1 moves the equilibrium from point A to point B , while merger M_2 moves the equilibrium from point A to point C . But, conditional on merger M_1 taking place, merger M_2 moves the equilibrium from point B to point D along $b(\cdot; \bar{c}_{M_1})$. Since $\partial b(\cdot; \bar{c}_{M_1})/\partial Q_{-i} \in (-1, 0)$, aggregate output must increase. That is, conditional on merger M_1 taking place, merger M_2 remains CS-increasing. Moreover, we know from Corollary 1 it also remains profitable. Using the same type of argument, the reverse is also true: conditional on merger M_2 taking place, the merger M_1 remains CS-increasing and profitable.

Figure 4 illustrates the case in which both mergers are CS-decreasing in isolation. Conditional on the other merger taking place, each merger remains CS-decreasing. For instance, conditional on merger M_1 taking place, merger M_2 moves the equilibrium from point B to point D along $b(\cdot; \bar{c}_{M_1})$. Since $\partial b(\cdot; \bar{c}_{M_1})/\partial Q_{-i} \in (-1, 0)$, it follows that the merger reduces industry output.

We now turn to the interaction between mergers that have opposite effects on consumer surplus if implemented in isolation. Specifically, suppose that merger M_1 is CS-nondecreasing (and therefore profitable) in isolation, while merger M_2 is CS-decreasing in isolation. Figure 5 illustrates that merger M_2 can become CS-increasing (and therefore strictly profitable) conditional on merger M_1 occurring. In isolation, merger M_2 moves the equilibrium from point A to point C along $r_{M_2}(\cdot)$, and thus decreases industry output. But after merger M_1 has taken place, merger M_2 moves the equilibrium from point B to point D along $b(\cdot; \bar{c}_{M_1})$, and thus increases industry output.

When this occurs, we can say the following:

Proposition 2 *Suppose that merger M_1 is CS-nondecreasing in isolation, while merger M_2 is CS-decreasing in isolation but CS-nondecreasing once merger M_1 has taken place. Then:*

- (i) *merger M_1 is CS-increasing (and therefore strictly profitable) conditional on merger M_2 taking place;*

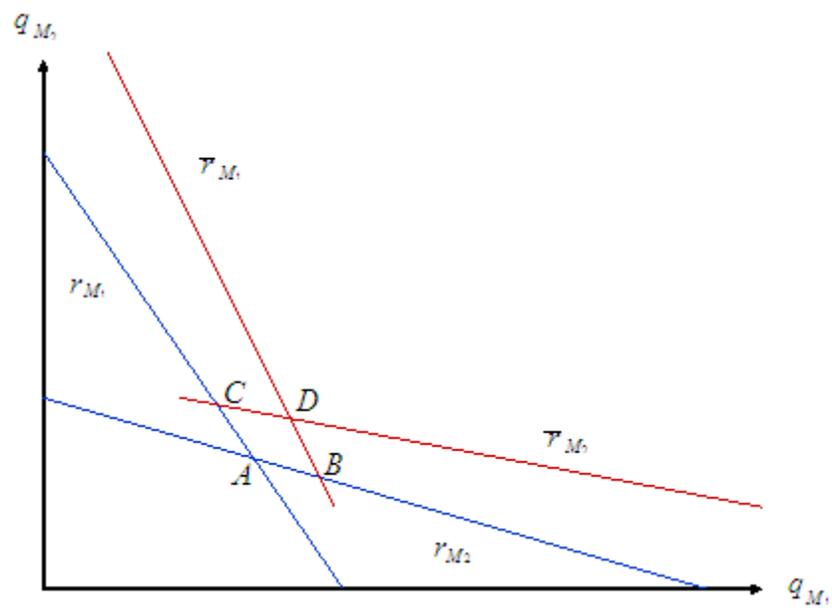


Figure 3: Each merger is CS-increasing in isolation and remains so if the other merger takes place.

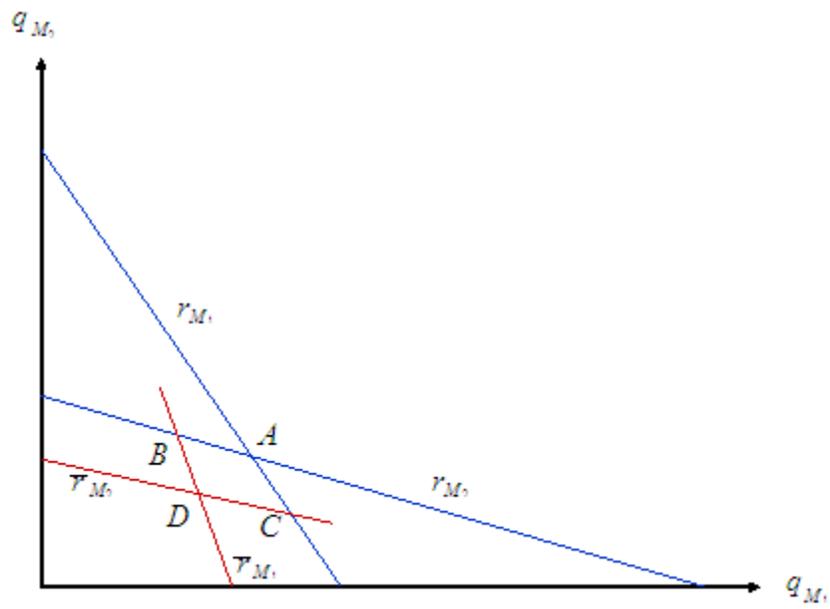


Figure 4: Each merger is CS-decreasing in isolation and remains so if the other takes place.

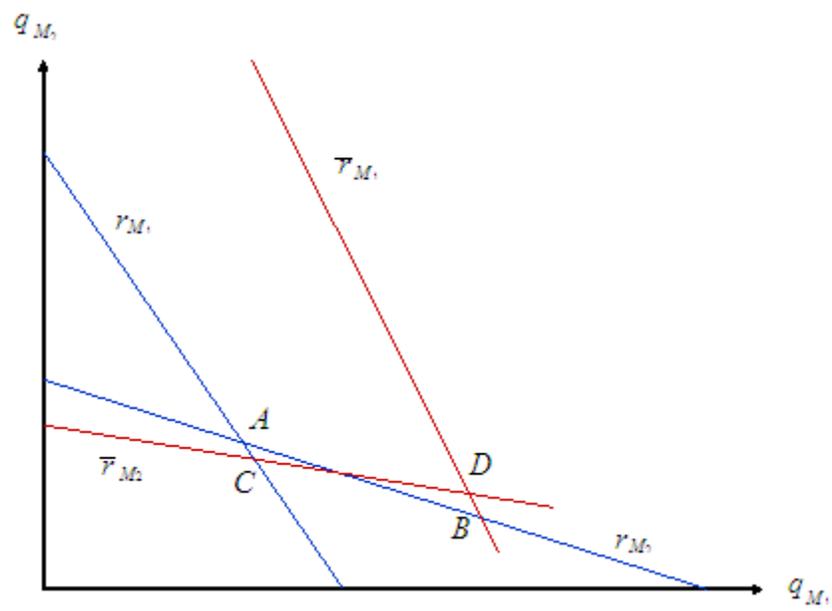


Figure 5: A CS-decreasing merger becomes CS-increasing after a CS-increasing merger takes place.

- (ii) *the joint profit of the firms involved in merger M_1 is strictly larger if both mergers take place than if neither merger takes place.*

Proof. Note, first, that if merger M_1 changes merger M_2 from CS-decreasing to CS-nondecreasing, then merger M_1 must in fact be CS-increasing in isolation [by Proposition 1(ii)]. Consider implementing merger M_1 first followed by merger M_2 . By hypothesis, consumer surplus weakly increases at each step, so the combined effect on consumer surplus of the two mergers is nonnegative. Suppose we now reverse the order and implement merger M_2 first. Since the combined effect of the two mergers on consumer surplus is nonnegative while the effect of merger M_2 is strictly negative, consumer surplus must strictly increase when merger M_1 is implemented following merger M_2 . Hence, part (i) must hold: merger M_1 is CS-increasing (and therefore strictly profitable) conditional on merger M_2 taking place.

To see that part (ii) holds, suppose that merger M_2 is implemented first. Since merger M_2 is CS-decreasing in isolation, it must weakly increase the profit of each firm $i \in M_1$ [the joint output of all firms other than i must decrease, otherwise the fact that $\partial b(\cdot; c_i)/\partial Q_{-i} \in (-1, 0)$ would imply that aggregate output increases]. Since merger M_1 is strictly profitable given merger M_2 , the sequence of mergers must strictly increase the joint profit of the firms in M_1 . ■

The result is illustrated in Figure 5, where merger M_1 is CS-increasing (and hence strictly profitable) in isolation and remains so conditional on merger M_2 taking place: it moves the equilibrium from point C to point D along $b(\cdot; \bar{c}_{M_2})$.

Remark 1 *Observe that the logic of Proposition 2 can be extended to cases with a merger M_1 that is CS-nondecreasing in isolation and a collection of mergers M_2, \dots, M_K that are each CS-decreasing in isolation but form a sequence that is CS-nondecreasing at each step after merger M_1 has taken place. In such cases, merger M_1 is CS-increasing (and therefore strictly profitable) given that mergers M_2, \dots, M_K have taken place, and the joint profit of the firms involved in merger M_1 is strictly larger if all of these mergers take place than if none do. We will use this extension of Proposition 2 in Section 3.*

3 CS-Maximizing Merger Review

In this section, we consider the optimal merger approval policy for an antitrust authority concerned with maximizing discounted consumer surplus when multiple disjoint mergers may be proposed over time. We will show that, in the Cournot model of Section 2, a consumer surplus-oriented antitrust authority can achieve its optimal outcome using a myopic policy that approves mergers if and only if they are CS-nondecreasing at the time of approval.

As before, we denote the set of firms by N . The set of possible mergers are those in set $\mathbb{A} \equiv \{M_1, \dots, M_K\}$, where $M_k \subseteq N$ is a set of firms that may merge. We assume that possible mergers are disjoint; that is, $M_j \cap M_k = \emptyset$ for $j \neq k$. Thus, no firm has the possibility of being part of more than one merger. The merger process lasts for T periods. At the start of each period t ,

merger M_k may become feasible with probability $p_{kt} \in [0, 1]$, where $\sum_t p_{kt} \leq 1$.⁷ Conditional on merger M_k becoming feasible in period t , the firms in M_k receive a random draw of their post-merger cost \bar{c}_{M_k} according to the distribution F_{kt} . This formulation embodies another form of disjointness in merger possibilities: merger M_k receives at most one efficiency realization throughout the merger process.

Within each period t there are n stages at which the antitrust authority can approve a merger. For simplicity, at most one merger can be approved at each stage. At the start of each period, all firms with feasible mergers decide whether to propose them or not. We assume that firms split the gains from their merger in some fixed proportion (the proportion does not matter).⁸ A merger is proposed if all of the merger partners agree to propose it. Given the weak dominance refinement we employ below, a merger is therefore proposed if it weakly raises the joint expected discounted expected profit of the potential merger partners. (We assume firms choose to propose a merger if indifferent.)

The antitrust authority observes that a particular merger is feasible and its efficiency (post-merger marginal cost) only once it is proposed. Firms observe their own merger possibility when it becomes feasible but, like the antitrust authority, observe the possibilities of other firms only when those mergers are proposed. Previously proposed but rejected mergers can be either withdrawn or proposed again, as can previously unproposed feasible mergers.⁹ Payoffs in each period depend only on the set of mergers approved at the end of the period. The antitrust authority and the firms discount future payoffs (consumer surplus or profit) according to the discount factor $\delta \leq 1$.

3.1 Static Merger Review

It will be useful to consider first merger review in a static setting, corresponding to the case in which $T = 1$. In this case, firms simultaneously propose mergers at the start of the period, and the antitrust authority then reviews them one at a time.

In Section 2, we examined the interaction between two mergers. For the purposes of this section, we start by noting some useful properties of the interactions among more than two mergers:

Lemma 2 (*Incremental Gain Lemma*)

(i) *Suppose that a set of mergers $\mathfrak{M} \equiv \{M_1, \dots, M_{J_1}\}$ has the property that every merger $M \in \mathfrak{M}$ is CS-nondecreasing if all of the other mergers in \mathfrak{M} (those in the set $\mathfrak{M} \setminus M$) have taken place. Then for any strict subset $Y \subset \mathfrak{M}$, there exists an $M' \in \mathfrak{M} \setminus Y$ that is CS-nondecreasing if all of the mergers in Y*

⁷Since a merger that results in a post-merger marginal cost above the marginal cost of the most efficient merging firm will never be approved, this “feasibility” may be viewed as the event of receiving a cost draw below that level.

⁸For simplicity, we do not formally model bargaining among the merger partners.

⁹In the model, we do not allow previously approved mergers to be dissolved. However, it follows from our arguments that no (approved) merged firm would want to do so.

have taken place. As a result, starting from Y , there is a sequencing of the mergers in $\mathfrak{M} \setminus Y$ that is CS-nondecreasing at each step.

(ii) Suppose that a sequence of mergers M_1, \dots, M_{J_1} is CS-nondecreasing at each step. Then each merger $M \in \mathfrak{M} \equiv \{M_1, \dots, M_{J_1}\}$ is CS-nondecreasing if all of the other mergers in \mathfrak{M} (those in the set $\mathfrak{M} \setminus M$) have taken place.

Proof. (i) Suppose the result is not true, so that every $M' \in \mathfrak{M} \setminus Y$ is CS-decreasing if all of the mergers in Y have taken place. Proposition 1(ii) implies that, taking the mergers in Y as given, for any sequencing of the mergers in the set $\mathfrak{M} \setminus Y$ the merger implemented at each step, including the last step, is CS-decreasing. But this contradicts the hypothesis that the last merger in the sequence is CS-nondecreasing if all of the other mergers in the set \mathfrak{M} have taken place.

Given the existence of $M' \in \mathfrak{M} \setminus Y$ that is CS-nondecreasing if all of the mergers in Y have taken place, we can update the subset Y to $Y \cup \{M'\} \subset \mathfrak{M}$ and apply the same argument again. Continuing iteratively identifies a sequencing of the mergers in $\mathfrak{M} \setminus Y$ that is CS-nondecreasing at each step starting from the subset Y .

(ii) Consider an arbitrary merger M_j in sequence M_1, \dots, M_{J_1} . We will show that M_j is CS-nondecreasing given that all of the mergers in $\mathfrak{M} \setminus M_j$ have taken place. For $k \geq 0$, define the set $\mathfrak{M}^k = \{M_i : i \leq k\}$. Suppose that (a_k) merger M_j is CS-nondecreasing given $\mathfrak{M}^k \setminus M_j$ and that (b_k) merger M_{k+1} is CS-nondecreasing given \mathfrak{M}^k . Observe that property (a_k) is true by hypothesis for $k = j$, and that property (b_k) holds by hypothesis for all k . We claim that properties (a_k) and (b_k) imply property (a_{k+1}) : M_j is CS-nondecreasing given $\mathfrak{M}^{k+1} \setminus M_j$. To see this, observe that if merger M_{k+1} is CS-nondecreasing given $\mathfrak{M}^k \setminus M_j$, property (a_{k+1}) follows from Proposition 1(i), while if merger M_{k+1} is CS-decreasing given $\mathfrak{M}^k \setminus M_j$ [which can hold only if $j \leq k$] then property (a_{k+1}) follows from Proposition 2(i) [and the assumption that M_{k+1} is CS-nondecreasing given \mathfrak{M}^k]. Applying induction we find that merger M_j is CS-nondecreasing given that all of the mergers in $\mathfrak{M} \setminus M_j$ have taken place [property (a_{J_1})]. ■

Lemma 3 Suppose that two distinct sets of mergers $\mathfrak{M}_1 \equiv \{M_1, \dots, M_{J_1}\}$ and $\mathfrak{M}_2 \equiv \{M_1, \dots, M_{J_2}\}$ with $\mathfrak{M}_1 \not\subseteq \mathfrak{M}_2$, not necessarily disjoint, each have the property that every merger $M \in \mathfrak{M}_i$ is CS-nondecreasing if all of the other mergers in \mathfrak{M}_i (those in the set $\mathfrak{M}_i \setminus M$) have taken place. Then:

(i) there is a merger $M'_1 \in \mathfrak{M}_1 \setminus (\mathfrak{M}_1 \cap \mathfrak{M}_2)$ that is CS-nondecreasing given that all of the mergers in \mathfrak{M}_2 have taken place;

(ii) the set of mergers $\mathfrak{M}_1 \cup \mathfrak{M}_2$ results in a level of consumer surplus that is at least as great as that of either set \mathfrak{M}_1 or set \mathfrak{M}_2 .

Proof. (i) Part (i) of the Incremental Gain Lemma [Lemma 2(i)] implies that there exists a merger $M'_1 \in \mathfrak{M}_1 \setminus (\mathfrak{M}_1 \cap \mathfrak{M}_2)$ that is CS-nondecreasing given that all of the mergers in $\mathfrak{M}_1 \cap \mathfrak{M}_2$ have taken place. It also implies that there is a sequencing of the mergers in $\mathfrak{M}_2 \setminus (\mathfrak{M}_1 \cap \mathfrak{M}_2)$, say M_{21}, \dots, M_{2J_2} , that is CS-nondecreasing at each step, given that the mergers in $\mathfrak{M}_1 \cap \mathfrak{M}_2$ have taken place.

Let $\mathfrak{M}^k = \{M_{2i} : i \leq k\}$. Proposition 1(i) implies that if merger M'_1 is CS-nondecreasing given that all the mergers in $(\mathfrak{M}_1 \cap \mathfrak{M}_2) \cup \mathfrak{M}^k$ have taken place, then [since by hypothesis merger $M_{2,k+1}$ is also CS-nondecreasing given that all of the mergers in $(\mathfrak{M}_1 \cap \mathfrak{M}_2) \cup \mathfrak{M}^k$ have taken place] M'_1 is also CS-nondecreasing given that all of the mergers in $(\mathfrak{M}_1 \cap \mathfrak{M}_2) \cup \mathfrak{M}^{k+1}$ have taken place. Since merger M'_1 is CS-nondecreasing if all of the mergers in $(\mathfrak{M}_1 \cap \mathfrak{M}_2) \cup \mathfrak{M}^0 = (\mathfrak{M}_1 \cap \mathfrak{M}_2)$ have taken place, applying induction yields the result (taking $k = J_1$).

(ii) We argue first that every merger in set $\mathfrak{M}_2 \cup \{M'_1\}$ is CS-nondecreasing if all of the other mergers in that set have taken place. Part (i) implies that this is true for merger M'_1 . Now consider any merger $M'_2 \in \mathfrak{M}_2$. By hypothesis, merger M'_2 is CS-nondecreasing given that all the mergers in set $\mathfrak{M}_2 \setminus M'_2$ have taken place. If merger M'_1 is also CS-nondecreasing if all of the mergers in set $\mathfrak{M}_2 \setminus M'_2$ have taken place, then Proposition 1(i) implies that merger M'_2 is CS-nondecreasing if all of the mergers in $(\mathfrak{M}_2 \setminus M'_2) \cup \{M'_1\} = (\mathfrak{M}_2 \cup \{M'_1\}) \setminus M'_2$ have taken place. If, instead, merger M'_1 is CS-decreasing if all of the mergers in set $\mathfrak{M}_2 \setminus M'_2$ have taken place, then Proposition 2(i) implies that this same property holds. This establishes that every merger in $\mathfrak{M}_2 \cup \{M'_1\}$ is CS-nondecreasing if all of the other mergers in that set have taken place. Moreover, by part (i), the level of consumer surplus with set $\mathfrak{M}_2 \cup \{M'_1\}$ is at least as large as with set \mathfrak{M}_2 .

Next, note that sets \mathfrak{M}_1 and $\mathfrak{M}_2 \cup \{M'_1\}$ satisfy the hypotheses of the Lemma. So we can apply the argument again for these two sets. Continuing iteratively in this fashion we establish the result by adding to \mathfrak{M}_2 a sequencing of the mergers in $\mathfrak{M}_1 \setminus (\mathfrak{M}_1 \cap \mathfrak{M}_2)$ that is CS-nondecreasing at each step. This establishes that the level of consumer surplus is at least as high with set $\mathfrak{M}_1 \cup \mathfrak{M}_2$ as with set \mathfrak{M}_2 . We also need to show that the level of consumer surplus in $\mathfrak{M}_1 \cup \mathfrak{M}_2$ is at least as large as in set \mathfrak{M}_1 . If $\mathfrak{M}_1 \supseteq \mathfrak{M}_2$, so that $\mathfrak{M}_1 \cup \mathfrak{M}_2 = \mathfrak{M}_1$, this follows immediately. If instead $\mathfrak{M}_1 \not\supseteq \mathfrak{M}_2$, then we can repeat the argument above with the roles of \mathfrak{M}_1 and \mathfrak{M}_2 reversed to establish the result. ■

We now define what we mean by a myopic merger review policy:¹⁰

Definition 1 *A myopic CS-based merger policy approves at each stage a proposed merger that is CS-nondecreasing given the market structure at the start of that stage, if any such mergers exist.*

A myopic CS-based merger policy results in a sequence of merger approvals that are each CS-nondecreasing at the time of their approval, and all proposed mergers that are not approved are CS-decreasing given the final set of approved mergers.

In the static (one-period) setting, the only thing that matters for the antitrust authority's payoff is the set of approved mergers at the end of the period. This, of course, depends on the realization of the set of feasible mergers (including their cost realizations). The antitrust authority does not know which mergers are feasible. It only sees proposed mergers. Nonetheless, we will see that any myopic CS-based rule maximizes consumer surplus for each realization

¹⁰Note that, for simplicity, we resolve indifference in favor of approval.

of the set of feasible mergers. That is, the antitrust authority does as well as if it knew the set of feasible mergers and could implement whichever ones it wanted. To this end, we introduce the following notion of ex-post optimality, defined relative to a particular realization of the set of feasible mergers.

Definition 2 *Let \mathfrak{F} denote the set of feasible mergers (including their cost realizations). A set of approved mergers \mathfrak{M} is **CS-maximizing for \mathfrak{F}** if it maximizes consumer surplus given \mathfrak{F} . It is a **largest CS-maximizing set for \mathfrak{F}** if it is not contained in any other set that is CS-maximizing for \mathfrak{F} .*

Observe that both the largest CS-maximizing set and the set of mergers resulting from a myopic CS-based merger policy have the property that every approved merger is CS-nondecreasing given the set of approved mergers, and all unapproved mergers are CS-decreasing given the set of approved mergers. This is immediate for the largest CS-maximizing set: otherwise we could either raise consumer surplus by no longer approving a merger that is CS-decreasing given the other approved mergers, or we could find a larger CS-maximizing set by approving an additional merger that is CS-nondecreasing given the other approved mergers. For the set of mergers resulting from a myopic CS-based merger policy this property follows from part (ii) of the Incremental Gain Lemma [Lemma 2(ii)], which says that any set of mergers that results from a sequence of CS-nondecreasing merger approvals has the property that each approved merger is CS-nondecreasing given all the other approved mergers.

The properties of merger interactions we have identified imply that the largest CS-maximizing set is unique and increasing in the set of feasible mergers:

Lemma 4 *For each set of feasible mergers \mathfrak{F} there is a unique largest CS-maximizing set $\mathfrak{M}^*(\mathfrak{F})$. Moreover, if $\mathfrak{F} \subset \mathfrak{F}'$ then $\mathfrak{M}^*(\mathfrak{F}) \subseteq \mathfrak{M}^*(\mathfrak{F}')$.*

Proof. Suppose that \mathfrak{M} and \mathfrak{M}' are both largest CS-maximizing sets for \mathfrak{F} . Then the sets \mathfrak{M} and \mathfrak{M}' satisfy the hypothesis of Lemma 3. So, by Lemma 3(b), $\mathfrak{M} \cup \mathfrak{M}'$ is CS-maximizing as well, contradicting the assumption that \mathfrak{M} and \mathfrak{M}' are largest CS-maximizing sets for \mathfrak{F} .

For the second claim, suppose $\mathfrak{M}^*(\mathfrak{F}) \not\subseteq \mathfrak{M}^*(\mathfrak{F}')$. The sets $\mathfrak{M}^*(\mathfrak{F})$ and $\mathfrak{M}^*(\mathfrak{F}')$ satisfy the hypothesis of Lemma 3 and, since $\mathfrak{M}^*(\mathfrak{F}) \subseteq \mathfrak{F} \subset \mathfrak{F}'$, all mergers in set $\mathfrak{M}^*(\mathfrak{F})$ are feasible under \mathfrak{F}' . Thus, under \mathfrak{F}' , approval of the mergers in set $\mathfrak{M}^*(\mathfrak{F}) \cup \mathfrak{M}^*(\mathfrak{F}')$ is feasible and by Lemma 3(b) is also CS-maximizing, contradicting $\mathfrak{M}^*(\mathfrak{F}')$ being the largest CS-maximizing set for \mathfrak{F}' . ■

We next relate the outcome of a myopic CS-based approval policy to largest CS-maximizing sets:

Lemma 5 *Suppose the antitrust authority follows a myopic CS-based merger policy and $T = 1$. Then if $\tilde{\mathfrak{F}}$ is the set of proposed mergers, the set of approved mergers is $\mathfrak{M}^*(\tilde{\mathfrak{F}})$.*

Proof. Suppose that the set of proposed mergers is $\widehat{\mathfrak{F}}$. Let $\mathfrak{M} \subseteq \widehat{\mathfrak{F}}$ denote the set of mergers resulting from a myopic CS-based merger policy. If $\mathfrak{M} \not\subseteq \mathfrak{M}^*(\widehat{\mathfrak{F}})$, then Lemma 3(b) implies that the set $\mathfrak{M} \cup \mathfrak{M}^*(\widehat{\mathfrak{F}})$ is also CS-maximizing but larger than set $\mathfrak{M}^*(\widehat{\mathfrak{F}})$, a contradiction to $\mathfrak{M}^*(\widehat{\mathfrak{F}})$ being the largest CS-maximizing set under $\widehat{\mathfrak{F}}$. Hence, $\mathfrak{M} \subseteq \mathfrak{M}^*(\widehat{\mathfrak{F}})$. If $\mathfrak{M} \subset \mathfrak{M}^*(\widehat{\mathfrak{F}})$, Lemma 3(a) implies that once the mergers in \mathfrak{M} have been approved, there is a merger in $\mathfrak{M}^*(\widehat{\mathfrak{F}}) \setminus (\mathfrak{M} \cap \mathfrak{M}^*(\widehat{\mathfrak{F}}))$ that is CS-nondecreasing given that the mergers in \mathfrak{M} have taken place, contradicting \mathfrak{M} being the result of a myopic CS-based merger policy. ■

Lemma 5 implies that, when $T = 1$, if firms propose all feasible mergers then the outcome of any myopic CS-based merger policy is exactly the largest CS-maximizing set given the realized set of feasible mergers. The remaining issue is whether firms have an incentive to propose feasible mergers. The following proposition establishes that they do:

Proposition 3 *Suppose the antitrust authority follows a myopic CS-based merger policy and $T = 1$. It is then a weakly dominant strategy for firms with a feasible merger to propose it. When firms adopt this weakly dominant proposal strategy, the set of approved mergers is $\mathfrak{M}^*(\widehat{\mathfrak{F}})$, for every $\widehat{\mathfrak{F}}$.*

Proof. Given Lemma 4, we need only show that regardless of the proposal strategies being followed by other firms, the firms in merger M_k maximize their expected payoff by proposing their merger given that the antitrust authority uses a myopic CS-based policy. Let $\widehat{\mathfrak{F}}$ denote a realization of the set of proposed mergers if merger M_k is proposed (firms in other mergers may be using mixed strategies) and let $\widehat{\mathfrak{F}}_{-k} \equiv \widehat{\mathfrak{F}} \setminus M_k$ denote that realization without merger M_k included. By Lemma 4, $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k}) \subseteq \mathfrak{M}^*(\widehat{\mathfrak{F}})$. If $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k}) = \mathfrak{M}^*(\widehat{\mathfrak{F}})$, then the payoffs of firms in M_k are independent of whether they propose. Suppose instead that $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k}) \subset \mathfrak{M}^*(\widehat{\mathfrak{F}})$. We distinguish between two cases. First, suppose that $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k}) \cup M_k = \mathfrak{M}^*(\widehat{\mathfrak{F}})$. In this case, proposing merger M_k does not affect the other mergers that will be approved. Since $M_k \in \mathfrak{M}^*(\widehat{\mathfrak{F}})$, the merger is CS-nondecreasing and hence [by Corollary 1] profitable, given the other mergers [those in the set $\mathfrak{M}^*(\widehat{\mathfrak{F}}) \setminus M_k = \mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$] that will be approved. Second, suppose that $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k}) \cup M_k \subset \mathfrak{M}^*(\widehat{\mathfrak{F}})$. By part (i) of the Incremental Gain Lemma [Lemma 2(i)], there is a sequencing of the mergers in $\mathfrak{M}^*(\widehat{\mathfrak{F}}) \setminus \mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$ that is CS-nondecreasing at each step. However, since all of the mergers in this set other than M_k must be CS-decreasing given that the mergers in $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$ have taken place [otherwise they would have been in $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$], merger M_k must be CS-nondecreasing given that the mergers in $\mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$ have occurred and must be the first merger in this sequence. By Remark 1, the firms in M_k have a greater profit when all of the mergers in $\mathfrak{M}^*(\widehat{\mathfrak{F}}) \setminus \mathfrak{M}^*(\widehat{\mathfrak{F}}_{-k})$ are approved than when none are. Hence, it is strictly more profitable in this case for the firms to propose merger M_k . As a result, each firm involved in merger M_k has a weakly dominant strategy to propose it. ■

3.2 Dynamic Merger Review

We now extend the analysis to the dynamic setting, where $T > 1$. A realization of feasible mergers is now a sequence $\mathfrak{F} = (\mathfrak{F}_1, \dots, \mathfrak{F}_T)$ where $\mathfrak{F}_t \subseteq \mathfrak{F}_{t'}$ for $t' > t$. An outcome of the merger review process is a sequence of cumulatively approved mergers $\mathfrak{M} = (\mathfrak{M}_1, \dots, \mathfrak{M}_T)$ where $\mathfrak{M}_t \subseteq \mathfrak{M}_{t'}$ for $t' > t$ and $\mathfrak{M}_t \subseteq \mathfrak{F}_t$ for all t . We begin with a result characterizing approval sequences that maximize discounted consumer surplus for a given realized feasible sequence:

Lemma 6 *Given a realization of feasible mergers $\mathfrak{F} = (\mathfrak{F}_1, \dots, \mathfrak{F}_T)$, the approval sequence $\mathfrak{M} = [\mathfrak{M}^*(\mathfrak{F}_1), \dots, \mathfrak{M}^*(\mathfrak{F}_T)]$ maximizes discounted consumer surplus.*

Proof. Given the realized sequence of feasible mergers $\mathfrak{F} = (\mathfrak{F}_1, \dots, \mathfrak{F}_T)$, consider the problem of maximizing discounted consumer surplus. If we ignore the monotonicity constraint that the set of allowed mergers cannot shrink over time, we can choose the allowed set of mergers in any period independently from the mergers allowed in every other period. It is evident that in that case the approval sequence $\mathfrak{M} = [\mathfrak{M}^*(\mathfrak{F}_1), \dots, \mathfrak{M}^*(\mathfrak{F}_T)]$ is optimal since it maximizes consumer surplus in every period. However, since Lemma 4 implies that $\mathfrak{M}^*(\mathfrak{F}_1) \subseteq \dots \subseteq \mathfrak{M}^*(\mathfrak{F}_T)$, the monotonicity constraint is satisfied, so this is a solution to the constrained problem. ■

Lemma 6 shows that if feasible mergers always are proposed and the antitrust authority approves the mergers in set $\mathfrak{M}^*(\mathfrak{F}_t) \setminus \mathfrak{M}^*(\mathfrak{F}_{t-1})$ in each period t , then the outcome will maximize discounted consumer surplus given the actual realization of feasible mergers, even though the antitrust authority has no knowledge in any period of future feasible mergers.

Finally, we will argue that proposing a feasible merger is a weakly dominant strategy of a sort. Specifically, we consider subgame perfect equilibria for the firms given the antitrust authority's policy. We call a profile of strategies for the firms a *weakly dominant subgame perfect equilibrium* if in every period each firm is playing a weakly dominant strategy in the one-period game induced by (weakly dominant subgame perfect) continuation play. Our main result is:

Proposition 4 *Suppose the antitrust authority follows a myopic CS-based merger policy. Then all feasible mergers being proposed in each period after any history is a weakly dominant subgame perfect equilibrium. In this equilibrium, the outcome maximizes discounted consumer surplus given the realized sequence of feasible mergers $\mathfrak{F} = (\mathfrak{F}_1, \dots, \mathfrak{F}_T)$.*

Proof. We proceed by backward induction. Proposition 3 shows that the result is true in period T for any set of previously-approved mergers, \mathfrak{M}_{T-1} . Suppose it is true in every period $t > s$, and consider play in period s after the mergers in set \mathfrak{M}_{s-1} have previously been approved. Let $\mathfrak{M}^*(\mathfrak{F}|\mathfrak{M})$ denote the largest CS-maximizing set in a period given that the mergers in \mathfrak{M} have previously been approved and the set of feasible mergers (including those in \mathfrak{M}) is \mathfrak{F} . If all feasible mergers are proposed in period s , then the set of approved mergers in period s is $\mathfrak{M}^*(\mathfrak{F}_s|\mathfrak{M}_{s-1})$; if, instead, some are not proposed, then Lemmas

4 and 5 imply that the set of approved mergers is a subset of $\mathfrak{M}^*(\mathfrak{F}_s|\mathfrak{M}_{s-1})$. Moreover, by Lemma 4, $\mathfrak{M}^*(\mathfrak{F}_s|\mathfrak{M}_{s-1}) \subseteq \mathfrak{M}^*(\mathfrak{F}_t|\mathfrak{M}_{s-1})$ for all $t > s$. Since all feasible mergers are proposed in periods $t > s$, the set of approved mergers at the end of each period $t > s$ will therefore be $\mathfrak{M}^*(\mathfrak{F}_t|\mathfrak{M}_{s-1})$. In particular, the approvals in period s do not affect those in any later period. So the strategic considerations reduce to a single-period problem, and firms find proposing any feasible merger to be a weakly dominant strategy in period s for the same reasons as in Proposition 3 when $T = 1$. Applying induction establishes that it is a weakly dominant subgame perfect equilibrium for firms to propose all feasible mergers in every period after any history. Lemma 6 then implies that the outcome of this equilibrium maximizes discounted consumer surplus given the realized sequence of feasible mergers $\mathfrak{F} = (\mathfrak{F}_1, \dots, \mathfrak{F}_T)$. ■

4 Robustness (This section is still very rough and incomplete)

4.1 Mergers in the Bertrand Model

So far, we have assumed that firms compete in quantities. In this subsection, we show that our main results continue to hold when firms compete in prices rather than quantities.

As before, there are n firms producing a homogeneous good at constant returns to scale. Firm i 's marginal cost and price are denoted c_i and p_i . Market demand is given by $Q(p)$, where p is the lowest price offered by any firm. Demand is downward-sloping, $Q'(p) < 0$ for any $p > 0$ such that $Q(p) > 0$. Let $\iota(i|N) \in N$ denote the firm with the i th lowest marginal cost when the set of active firms is N , i.e., $c_{\iota(1|N)} \leq c_{\iota(2|N)} \leq \dots \leq c_{\iota(n|N)}$. (If a subset of firms have the same marginal cost, then the firms in this subset are ordered arbitrarily.) Assuming $Q(c^{(1)}) > 0$, firm $\iota(i|N)$'s equilibrium price $p_{\iota(i|N)}$ is given by

$$p_{\iota(i|N)} = \begin{cases} c_i & \text{if } 2 \leq i \leq n, \\ \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\} & \text{if } i = 1, \end{cases} \quad (7)$$

where $p^M(c) \equiv \arg \max_p [p - c] Q(p)$ is the (unconstrained) monopoly price of a firm with marginal cost c .¹¹ In equilibrium, all consumers purchase at price $p_{\iota(1|N)}$, and so consumer surplus is given by

$$CS(p_1, p_2, \dots, p_n) = \int_{p_{\iota(1|N)}}^{\infty} Q(p) dp. \quad (8)$$

Note that $CS(p_1, p_2, \dots, p_n)$ is independent of $p_{\iota(i|N)}$, $i > 1$, and decreasing in $p_{\iota(1|N)}$.

Consider a merger between a subset $M \subseteq N$ of firms. We will say that the merger is *cost-reducing* if the post-merger marginal cost of the merged entity,

¹¹While this is the most plausible equilibrium, there are typically other equilibria involving some firm(s) charging price(s) below marginal cost.

\bar{c}_M , is below the marginal cost of the most efficient merger partner, i.e., $\bar{c}_M < \min_{i \in M} c_i$. The merger is *cost-increasing* otherwise, i.e., if $\bar{c}_M \geq \min_{i \in M} c_i$. Let \bar{p}_M denote the post-merger price of the merged firm. From (8), the merger is CS-increasing if and only if $\bar{p}_M < p_{\iota(1|N)}$.

The distinction between cost-reducing and cost-increasing mergers turns out to be useful since the marginal cost of a firm that does not sell anything may still affect consumer surplus, depending on the marginal costs of rival firms. As a result, and in contrast to the Cournot model, it is no longer true that every merger that is CS-nondecreasing in isolation remains CS-nondecreasing conditional on another CS-nondecreasing merger taking place. To see this, suppose merger M_1 involves the firm with the lowest marginal cost, $\iota(1|N)$, and that, prior to any merger, firm $\iota(1|N)$ charges a price equal to the marginal cost of the firm the second-lowest marginal cost, $p_{\iota(1|N)} = c_{\iota(2|N)}$. Suppose also that the merger is cost-reducing but CS-neutral in isolation, $c_{\iota(2|N)} \geq \bar{c}_{M_1} > c_{\iota(1|N)}$. On the other hand, merger M_2 is cost-reducing and CS-increasing in isolation: the post-merger marginal cost satisfies $\bar{c}_{M_2} < c_{\iota(1|N)} < p^M(\bar{c}_{M_2})$. Hence, the merged entity M_2 will charge price $c_{\iota(1|N)}$ if M_1 does not take place but price $\min\{p^M(\bar{c}_{M_2}), \bar{c}_{M_1}\} > c_{\iota(1|N)}$ if M_1 has taken place. That is, the cost-increasing M_1 is CS-neutral in isolation but becomes CS-decreasing conditional on the CS-increasing M_2 taking place. Note that this issue does not arise in the Cournot model where every cost-increasing merger is CS-decreasing.

The following lemma states some useful properties of mergers.

Lemma 7 *Consider a merger between a subset M of firms.*

1. *If the merger is cost-reducing, it is weakly profitable (in that it weakly increases the joint profit of the firms in M).*
2. *If the merger is CS-increasing, it is a cost-reducing merger (and, therefore, weakly profitable).*
3. *If the merger is cost-reducing and CS-decreasing, it must involve both firms $\iota(1|N)$ and $\iota(2|N)$.*

Proof. To see Property 1, note that, in equilibrium, only firm $\iota(1|N)$ makes any profit before the merger (and only if $c_{\iota(1|N)} < c_{\iota(2|N)}$). Hence, any cost-reducing merger that does not involve firm (1) cannot decrease the joint profit of the merging firms. Suppose now the (cost-reducing) merger involves firm $\iota(1|N)$. In this case, the merger will not affect the equilibrium prices of the firms not involved in the merger, and so the cost-reducing merger must be profitable.

To see Property 2, let \bar{p}_M denote the post-merger price of the merged entity and assume the merger is CS-increasing, i.e., $\bar{p}_M < p_{\iota(1|N)}$. Suppose the merger involves firm $\iota(1|N)$ but not firm $\iota(2|N)$. Then, $\bar{p}_M = \min\{p^M(\bar{c}_M), c_{\iota(2|N)}\}$. Since $p^M(c)$ is strictly increasing in c , $\bar{p}_M < p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(1|N)}\}$ implies that the merger is cost-reducing, $\bar{c}_M < c_{\iota(1|N)}$. Suppose now the merger does not involve firm $\iota(1|N)$. Then, since $\bar{p}_M \geq \bar{c}_M$, $\bar{p}_M < p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\}$ implies that $\bar{c}_M < c_{\iota(2|N)}$, i.e., the merger is cost-reducing. Suppose finally the merger involves both firms $\iota(1|N)$ and $\iota(2|N)$.

Then, $\bar{p}_M = \min\{p^M(\bar{c}_M), c_{\iota(1|N \setminus M)}\}$, where $c_{\iota(1|N \setminus M)}$ is the marginal cost of the most efficient firm not involved in the merger. Since $c_{\iota(1|N) \setminus M} \geq c_{\iota(2|N)}$, $\bar{p}_M = \min\{p^M(\bar{c}_M), c_{\iota(1|N \setminus M)}\} < p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\}$ implies that $\bar{c}_M < c_{\iota(1|N)}$, i.e., the merger is cost-reducing.

To see Property 3, assume the merger is CS-decreasing, i.e., $\bar{p}_M > p_{\iota(1|N)}$. Since $p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\}$, it follows that the merger has to involve either firm $\iota(1|N)$ or firm $\iota(2|N)$, or both. Suppose the merger involves firm $\iota(1|N)$ but not firm $\iota(2|N)$. If $\bar{c}_M \leq c_{\iota(1|N)}$, then $\bar{p}_M = \min\{p^M(\bar{c}_M), c_{\iota(2|N)}\} \leq p_{\iota(1|N)}$; a contradiction. Hence, $\bar{c}_M > c_{\iota(1|N)}$, i.e., the merger is cost-increasing. Suppose now the merger involves firm $\iota(2|N)$ but not firm $\iota(1|N)$. If $\bar{c}_M \leq c_{\iota(2|N)}$, then $\bar{p}_M = \min\{p^M(\bar{c}_M), p^M(c_{\iota(1|N)}), \bar{c}_M\} \leq p_{\iota(1|N)}$; a contradiction. Hence, $\bar{c}_M > c_{\iota(2|N)}$, i.e., the merger is cost-increasing. It follows that if the merger is cost-reducing and CS-decreasing, it must involve both firms $\iota(1|N)$ and $\iota(2|N)$. ■

We now turn to the interaction between two disjoint mergers, M_1 and M_2 , where $M_1 \cap M_2 = \emptyset$. Let N denote the set of firms if neither merger takes place, N_i the set of firms after merger M_i (but not M_j , $j \neq i$) has taken place, and N_{12} the set of firms after both mergers have taken place. Since every CS-increasing merger is cost-reducing (Lemma 7), we will focus on cost-reducing mergers. As in the case of the Cournot model, there is a certain complementarity between mergers that change consumer surplus in the same direction.

Proposition 5 *The CS-effect of mergers is complementary:*

- (i) *If a (cost-reducing) merger is CS-nondecreasing in isolation, it remains CS-nondecreasing if another (cost-reducing) merger that is CS-nondecreasing in isolation takes place.*
- (ii) *If a merger is CS-decreasing in isolation, it remains CS-nonincreasing if another merger that is CS-decreasing in isolation takes place. Further, if a merger is cost-reducing and CS-decreasing in isolation, there cannot be another (disjoint) merger that is CS-decreasing in isolation.*

Proof. To see part (i), suppose to the contrary that the merger, say M_2 , becomes CS-decreasing if the other merger, say M_1 , takes place. Since M_2 is cost-reducing, the merger must involve (after M_1 has taken place) firms $\iota(1|N_1)$ and $\iota(2|N_1)$ (see Lemma 7), and $\min\{p^M(\bar{c}_{M_2}), c_{\iota(1|N_1 \setminus M_2)}\} > c_{\iota(2|N_1)}$, where $c_{\iota(1|N_1 \setminus M_2)}$ is the marginal cost of the most efficient firm not involved in merger M_2 (after merger M_1 has taken place). But since M_1 is cost-reducing, $\iota(1|N_1) = \iota(1|N)$ and $\iota(2|N_1) = \iota(2|N)$, i.e., M_2 must involve firms $\iota(1|N)$ and $\iota(2|N)$. Further, since M_2 is CS-nondecreasing in isolation, $\min\{p^M(\bar{c}_{M_2}), c_{\iota(1|N \setminus M_2)}\} \leq c_{\iota(2|N)} = c_{\iota(2|N_1)}$, where $c_{\iota(1|N \setminus M_2)}$ is the marginal cost of the most efficient firm not involved in merger M_2 before merger M_1 has taken place. Hence, $c_{\iota(1|N_1 \setminus M_2)} > c_{\iota(1|N \setminus M_2)}$. But M_1 is cost-reducing, and so $c_{\iota(1|N_1 \setminus M_2)} \leq c_{\iota(1|N \setminus M_2)}$, a contradiction.

To see part (ii), note that since M_i is CS-decreasing in isolation, M_i must involve either firm $\iota(1|N)$ or firm $\iota(2|N)$, or both. This holds for each of the two

mergers, and so one of the two mergers, say M_1 , must involve firm $\iota(1|N)$, while M_2 involves firm $\iota(2|N)$. Next, note that $p_{\iota(1|N)} = c_{\iota(2|N)}$ and $\bar{c}_{M_2} > c_{\iota(2|N)}$ since, otherwise, if $p_{\iota(1|N)} = p^M(c_{\iota(1|N)})$ or $\bar{c}_{M_2} \leq c_{\iota(2|N)}$, M_2 could not be CS-decreasing. Since M_1 is CS-decreasing in isolation, $\bar{c}_{M_1} > c_{\iota(2|N)} \geq c_{\iota(1|N)}$. Hence, each of the two mergers is cost-increasing. From Lemma 7, it follows that each merger can never become CS-increasing. Finally, note that if merger M_i is cost-reducing and CS-increasing, it must, from Lemma 7, involve firms $\iota(1|N)$ and $\iota(2|N)$. But then the other merger M_j cannot be CS-decreasing. ■

We now turn to the interaction between mergers that, in isolation, affect consumer surplus in opposite directions.

Proposition 6 *Suppose that merger M_1 is CS-increasing (and therefore cost-reducing) in isolation, while merger M_2 is CS-decreasing in isolation but CS-increasing once merger M_1 has taken place. Then:*

- (i) *Merger M_2 is a cost-reducing merger.*
- (ii) *Merger M_1 is CS-increasing conditional on merger M_2 taking place.*
- (iii) *The joint profits of the firms involved in merger M_1 are weakly higher if both mergers take place than if neither merger takes place.*

Proof. To see part (i), suppose otherwise that M_2 is cost-increasing. But then, from Lemma 7, M_2 can never be CS-increasing; a contradiction.

The proof of part (ii) is identical to that of part (i) of Proposition 2.

To see part (iii), note that since M_2 is a cost-reducing merger that is CS-decreasing in isolation, it must involve firms $\iota(1|N)$ and $\iota(2|N)$. Hence, if no merger takes place, the joint profit of the firms in M_1 is zero. ■

We now turn to the optimal merger approval policy for an antitrust authority concerned with maximizing (discounted) consumer surplus when multiple disjoint mergers may be proposed over time, as described in Section 3. Since only the most efficient firm makes any sales in the Bertrand model, a myopic CS-based merger policy needs to distinguish between cost-reducing and cost-increasing mergers. We therefore modify our definition of a myopic CS-based merger policy as follows:

Definition 3 *A myopic CS-based merger policy approves at each stage a proposed merger that is cost-reducing and CS-nondecreasing given the market structure at the start of that stage, if any such mergers exist.*

It can readily be verified that, using this modified definition, Propositions 3 and 4 carry over to the Bertrand model. In particular, in the *weakly dominant subgame perfect equilibrium* firms propose every feasible merger, and so the set of approved mergers in every period t is $\mathfrak{M}^*(\mathfrak{F}_t)$. The outcome maximizes discounted consumer surplus, given the actual realized sequence of feasible mergers.

4.2 Mergers with Differentiated Goods

4.3 Non-Constant Returns to Scale

4.4 Overlapping Mergers

4.5 Aggregate Surplus Standard

While the legal standard of merger policy in the U.S. and the EU is close to being a consumer surplus standard, economists typically focus on aggregate (or total) surplus as the welfare criterion. In this subsection, we investigate whether our main results continue to hold when the antitrust authority adopts an aggregate surplus standard. In doing so, we consider the homogeneous-goods Bertrand model of Section 4.1.

Adopting the notation (and assumptions) of Section 4.1, aggregate (or total) surplus is given by

$$AS(p_1, p_2, \dots, p_n; c_1, c_2, \dots, c_n) = \int_{p_{\iota(1|N)}}^{\infty} Q(p) dp + [p_{\iota(1|N)} - c_{\iota(1|N)}]Q(p_{\iota(1|N)}), \quad (9)$$

where $p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\}$ is the equilibrium price of the most efficient firm. Note that $\partial AS(\cdot)/\partial p_{\iota(1|N)} \leq 0$, $\partial AS(\cdot)/\partial c_{\iota(1|N)} \leq 0$, $dAS(\cdot)/dc_{\iota(1|N)} \leq 0$, $dAS(\cdot)/dc_{\iota(2|N)} \leq 0$, and $dAS(\cdot)/dc_{\iota(k|N)} = 0$ for $k > 2$.

Consider a merger between a subset $M \subseteq N$ of firms. Following our previous notation, we will say that the merger is *AS-neutral* if the merger does not affect aggregate surplus. Similarly, we will say that a merger is *AS-increasing* [*AS-decreasing*], if aggregate surplus following the merger is higher [lower] than before. Finally, a merger is *AS-nondecreasing* [*AS-nonincreasing*] if it is not AS-decreasing [AS-increasing].

The following lemma shows that the set of cost-reducing and AS-nondecreasing mergers is a superset of the set of cost-reducing and CS-nondecreasing mergers, and that every cost-reducing merger that is AS-nondecreasing but CS-decreasing must involve firms $\iota(1|N)$ and $\iota(2|N)$.

Lemma 8 *Consider a merger between a subset M of firms.*

1. *If the merger is AS-increasing, it is cost-reducing.*
2. *If the merger is cost-reducing and CS-nondecreasing, it is AS-nondecreasing.*
3. *If a cost-reducing and AS-nondecreasing merger is CS-decreasing, it involves firms $\iota(1|N)$ and $\iota(2|N)$.*
4. *If a cost-reducing merger is AS-decreasing, it involves firms $\iota(1|N)$ and $\iota(2|N)$.*
5. *If the merger is AS-decreasing, it is CS-nonincreasing. If it is AS-decreasing and CS-neutral, it involves firm $\iota(1|N)$.*

Proof. Property 1 follows immediately from the observation that $dAS(\cdot)/dc_{\iota(1|N)} \leq 0$, $dAS(\cdot)/dc_{\iota(2|N)} \leq 0$, and $dAS(\cdot)/dc_{\iota(k|N)} = 0$ for $k > 2$.

Property 2 follows from $\partial AS(\cdot)/\partial p_{\iota(1|N)} \leq 0$, $\partial AS(\cdot)/\partial c_{\iota(1|N)} \leq 0$, and $\partial AS(\cdot)/\partial c_{\iota(k|N)} = 0$ for all $k > 1$.

To see Property 3, note that since $p_{\iota(1|N)} = \min\{p^M(c_{\iota(1|N)}), c_{\iota(2|N)}\}$, any cost-reducing merger that does not involve firms $\iota(1|N)$ and $\iota(2|N)$ is CS-nondecreasing (see also Lemma 7).

To see Property 4, suppose otherwise that the merger does not involve firms $\iota(1|N)$ and $\iota(2|N)$. If the marginal cost of the merged entity satisfies $\bar{c}_M \geq c_{\iota(2|N)}$, the merger is AS-neutral; a contradiction. If, on the other hand, $\bar{c}_M < c_{\iota(2|N)}$, the (cost-reducing) merger is CS-nondecreasing. From Property 2, it follows that the merger is AS-nondecreasing; a contradiction.

To see Property 5, note that, from Property 2, a merger that is cost-reducing and AS-decreasing merger must be CS-decreasing. Suppose now the merger is cost-increasing, i.e., $\bar{c}_M \geq c_{\iota(1|N)}$. From Lemma 7, it must therefore be CS-nonincreasing. Since $dAS(\cdot)/dc_{\iota(k|N)} = 0$ for $k > 2$, the merger must involve either firm $\iota(1|N)$, firm $\iota(2|N)$, or both for it to be AS-decreasing. Suppose the merger involves firm $\iota(2|N)$ but not firm $\iota(1|N)$. Then, since $\partial AS(\cdot)/\partial c_{\iota(k|N)} = 0$ for $k > 1$ and $\partial AS(\cdot)/\partial p_{\iota(1|N)} \leq 0$, the post-merger price of firm $\iota(1|N)$, $\bar{p}_{\iota(1|N)}$, must be higher than its pre-merger price, $\bar{p}_{\iota(1|N)} > p_{\iota(1|N)}$ for the merger to be AS-decreasing. But this means that the merger is CS-decreasing. Hence, if the merger is AS-decreasing and CS-neutral, it must involve firm $\iota(1|N)$. ■

We now turn to the interaction between two disjoint mergers, M_1 and M_2 , where $M_1 \cap M_2 = \emptyset$. The following proposition shows that there is a certain complementarity between mergers that change aggregate surplus in the same direction.

Proposition 7 *The AS-effect of mergers is complementary:*

- (i) *If a (cost-reducing) merger is AS-nondecreasing in isolation, it remains AS-nondecreasing if another (cost-reducing) merger that is AS-nondecreasing in isolation takes place.*
- (ii) *If a merger is AS-decreasing in isolation, it remains AS-nonincreasing if another merger that is AS-decreasing in isolation takes place. Further, if a merger is cost-reducing and AS-decreasing in isolation, there cannot be another (disjoint) merger that is AS-decreasing in isolation.*

Proof. Consider part (i). If both mergers are CS-nondecreasing in isolation, then, from Proposition 5, each merger remains CS-nondecreasing conditional on the other merger taking place. Lemma 8, Property 2, then implies that each merger remains AS-nondecreasing. Indeed, if neither merger involves both firms $\iota(1|N)$ and $\iota(2|N)$, then, from Lemma 8, Property 3, then both mergers are CS-nondecreasing in isolation. Suppose now instead that one merger, say M_1 , involves both firms $\iota(1|N)$ and $\iota(2|N)$ and is CS-decreasing in isolation. This implies that the other merger, M_2 , must be CS-nondecreasing in isolation as otherwise it would not be AS-nondecreasing in isolation. Note that, prior to

merging, the firms in M_2 do not make any sales, independently of whether or not the merger M_1 takes place. Further, M_2 is cost-reducing, and $dAS(\cdot)/dc_{\iota(k|N)} \leq 0$ for any k . This implies that M_1 must remain AS-nondecreasing conditional on M_2 taking place. Consider now M_2 , conditional on M_1 taking place. Since M_2 does not involve both $\iota(1|N_1)$ and $\iota(2|N_1)$ and since it is cost-reducing, Lemma 7 implies that M_2 is CS-nondecreasing conditional on M_1 taking place. From Lemma 8, it follows that M_2 is AS-nondecreasing conditional on M_1 taking place.

Consider now part (ii). Suppose one of the mergers, say M_1 , involves both firms $\iota(1|N)$ and $\iota(2|N)$. But then merger M_2 cannot be AS-decreasing. To see this, note that if $\bar{c}_{M_2} \geq c_{\iota(2|N)}$, the merger is AS-neutral. If, on the other hand, $\bar{c}_{M_2} < c_{\iota(2|N)}$, merger M_2 is cost-reducing and CS-nondecreasing. From Lemma 8, Property 2, the merger is thus AS-nondecreasing. Hence, neither merger can involve both firms $\iota(1|N)$ and $\iota(2|N)$. On the other hand, if a merger does not involve either firm $\iota(1|N)$ or firm $\iota(2|N)$, or both, it cannot be AS-decreasing since $dAS(\cdot)/dc_{\iota(k|N)} = 0$ for $k > 2$. Hence, one of the two mergers, say M_1 , must involve firm $\iota(1|N)$, while merger M_2 involves firm $\iota(2|N)$. Lemma 8, Property 5, then implies that M_2 is CS-decreasing in isolation. Hence, prior to both mergers, $p_{\iota(1|N)} = c_{\iota(2|N)}$ (since, otherwise, if $p_{\iota(1|N)} < c_{\iota(2|N)}$, M_2 could not be CS-decreasing) and $\bar{c}_{M_2} > c_{\iota(2|N)}$, i.e., M_2 is cost-increasing. Since M_1 is AS-decreasing in isolation and does not involve firm $\iota(2|N)$, it must be cost-increasing (Lemma 8, Property 4). But Lemma 8, Property 1, implies that a cost-increasing merger must remain AS-nonincreasing.

Finally, note that if merger M_1 is cost-reducing and AS-decreasing in isolation, it must involve firms $\iota(1|N)$ and $\iota(2|N)$ (Lemma 8, Property 4). But, as shown above, this implies that merger M_2 , in isolation, is AS-nondecreasing. ■

We now turn to the interaction between mergers that, in isolation, affect consumer surplus in opposite directions.

Proposition 8 *Suppose that merger M_1 is AS-increasing (and therefore cost-reducing) in isolation, while merger M_2 is AS-decreasing in isolation but AS-increasing once merger M_1 has taken place. Then:*

- (i) *Merger M_2 is a cost-reducing merger.*
- (ii) *Merger M_1 is AS-increasing conditional on merger M_2 taking place.*
- (iii) *The joint profits of the firms involved in merger M_1 are weakly higher if both mergers take place than if neither merger takes place.*

Proof. Part (i) follows immediately from Lemma 8, Property 1.

The proof of part (ii) is along the same lines as that of part (i) of Proposition 2.

To see part (iii), note that since M_2 is a cost-reducing merger that is AS-decreasing in isolation, it must involve firms $\iota(1|N)$ and $\iota(2|N)$ (see Lemma 8, Property 4). Hence, if no merger takes place, the joint profit of the firms in M_1 is zero. ■

We now turn to the optimal merger approval policy for an antitrust authority concerned with maximizing (discounted) aggregate surplus when multiple disjoint mergers may be proposed over time. The extensive form of the game is described in Section 3, but we replace the myopic CS-based merger policy considered there by the following myopic AS-based merger policy:

Definition 4 *A myopic AS-based merger policy approves at each stage a proposed merger that is cost-reducing and AS-nondecreasing given the market structure at the start of that stage, if any such mergers exist.*

It can readily be verified that, under this myopic AS-based merger policy, all feasible mergers being proposed in each period after any history is a weakly dominant subgame perfect equilibrium. In this equilibrium, the set of approved mergers in every period t is the AS-maximizing set given the set of feasible mergers \mathfrak{F}_t . Further, the outcome maximizes discounted aggregate surplus, given the actual realized sequence of feasible mergers.

5 Conclusion

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